

Chapter 13

Breakeven Analysis

Solutions to Problems

13.1 (a) $Q_{BE} = 1,000,000 / (8.50 - 4.25) = 235,294$ units

(b) Profit = R - TC
 $= 8.50Q - 1,000,000 - 4.25Q$

at 200,000 units: Profit = $8.50(200,000) - 1,000,000 - 4.25(200,000)$
 $= \$-150,000$ (loss)

at 350,000 units: Profit = $\$487,500$

For computer plot: Develop an Excel graph for different Q values using the relation:

$$\text{Profit} = 4.25Q - 1,000,000$$

13.2 One is linear and the other is parabolic. Another is two parabolic. The curves would have the intersecting at real number points to ensure the 2 breakeven points.

13.3 Set revenue at efficiency E equal to the total cost

$$12,000(E)(250) = 15,000,000(A/P, 1\%, 20) + (4,100,000)E^{1.8}$$

$$3,000,000(E) = 15,000,000(0.01435) + (4,100,000)E^{1.8}$$

$$3,000,000(E) - 4,100,000E^{1.8} = 215,250$$

Solve for E by trial and error:

at E = 0.55: $252,227 > 215,250$

at E = 0.57: $219,409 > 215,250$

at E = 0.58: $202,007 < 215,250$

$$E = 0.572 \text{ or } 57.2\% \text{ minimum removal efficiency}$$

13.4 Using Equation [13.2] on a per month basis.

(a) $Q_{BE} = (4,000,000/12) / (39.95 - 24.75) = 333,333.3/15.2$

= 21,930 units/month

(b) In Equation [13.3] in Example 13.1 divide by Q to get profit (loss) per unit.

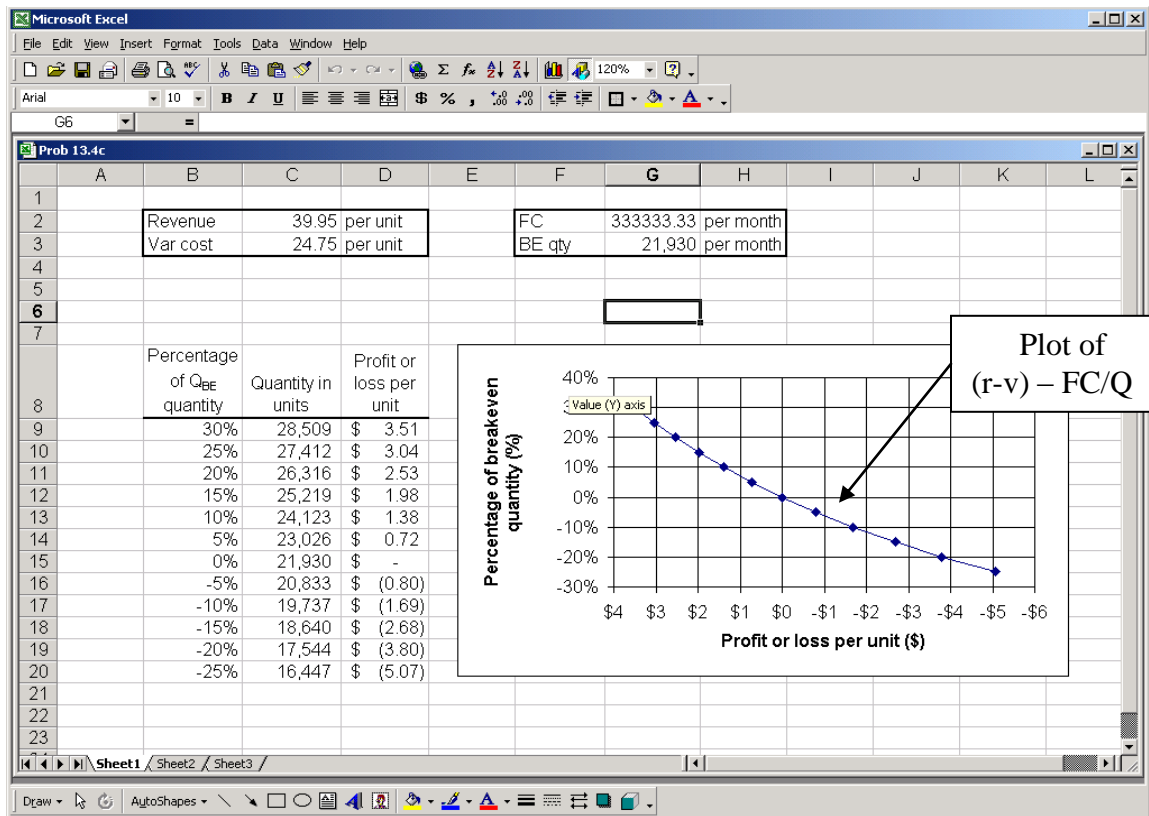
$$\text{Profit (loss)} = (r-v) - FC/Q$$

$$\begin{aligned} 10\% \text{ below } Q_{BE} : \text{ Loss} &= (r-v) - FC/Q \\ &= (39.95 - 24.75) - (333,333.3)/(21,930)(0.9) \\ &= 15.20 - 16.89 \\ &= \$-1.69 \text{ per unit} \end{aligned}$$

$$\begin{aligned} 10\% \text{ above } Q_{BE} : \text{ Profit} &= (r-v) - FC/Q \\ &= (39.95 - 24.75) - (333,333.3)/(21,930)(1.1) \\ &= 15.20 - 13.82 \\ &= \$ 1.38 \text{ per unit} \end{aligned}$$

(c) To plot the profit or loss per unit, use the equation in part (b).

$$\text{Profit or loss} = (r-v) - FC/Q$$



13.5 From Equation [13.4], plot $C_u = 160,000/Q + 4$. Plot is shown below.

(a) If $C_u = \$5$, from the graph, Q is approximately 160,000. If Q is determined by Equation [13.4], it is

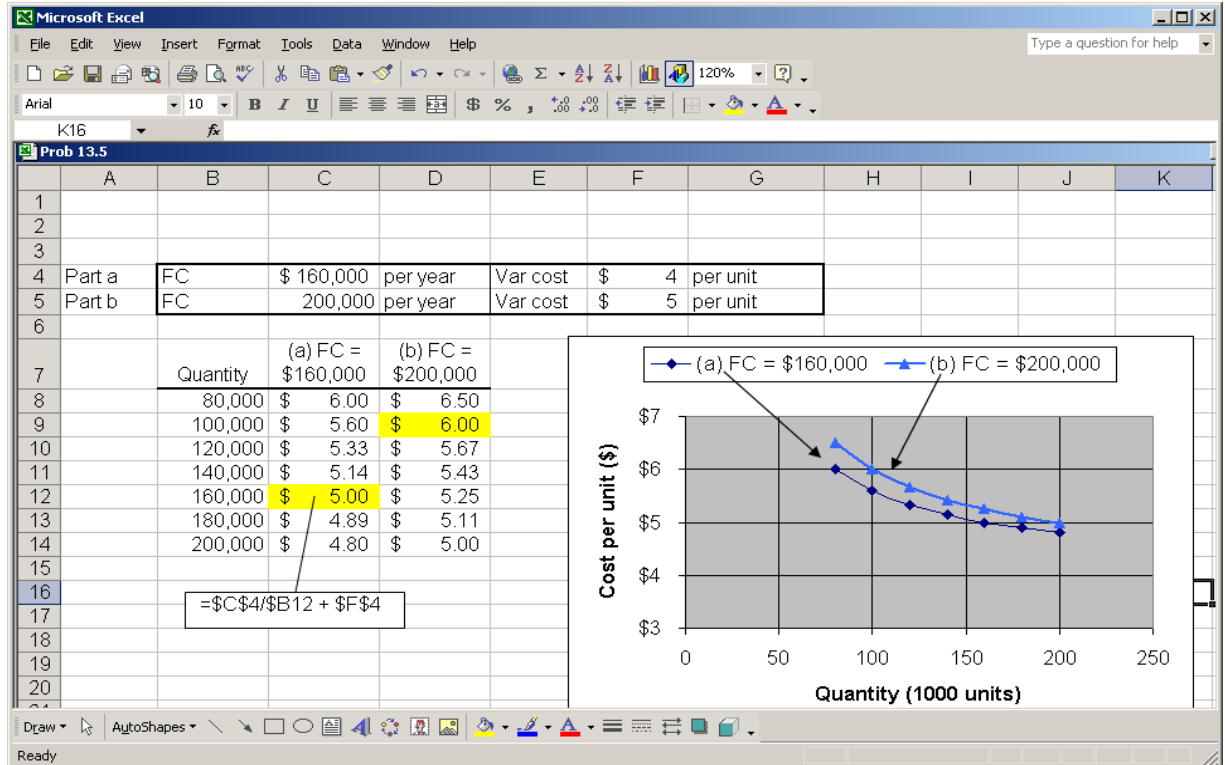
$$5 = 160,000/Q + 4$$

$$Q = 160,000/1 = 160,000 \text{ units}$$

(b) From the plot, or by equation, $Q = 100,000$ units.

$$C_u = 6 = 200,000/Q + 4$$

$$Q = 200,000/2 = 100,000 \text{ units}$$



13.6 (a) $Q_{BE} = \frac{775,000}{3.50 - 2} = 516,667$ calls per year

This is 37% of the center's capacity

(b) Set $Q_{BE} = 500,000$ and determine r at $v = \$2$ and $FC = 0.5(900,000)$.

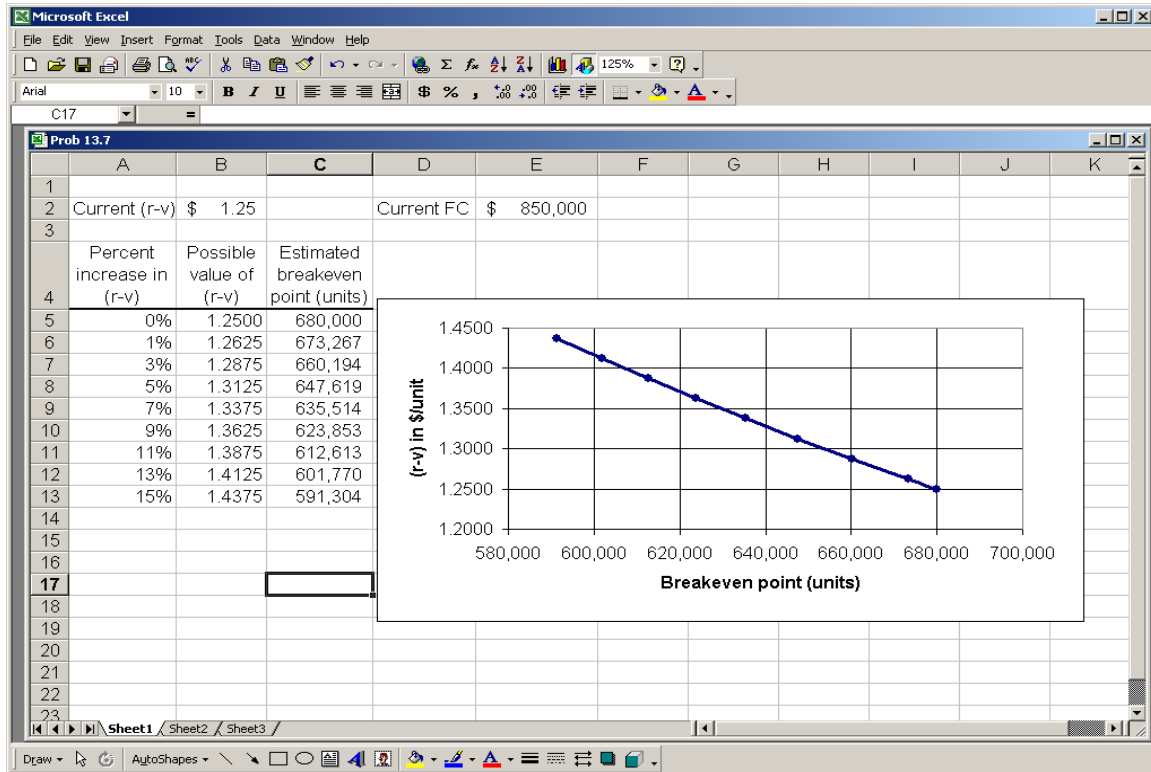
$$500,000 = \frac{450,000}{r - 2}$$

$$r - 2 = \frac{450,000}{500,000}$$

$$r = 0.9 + 2 = \$2.90 \text{ per call}$$

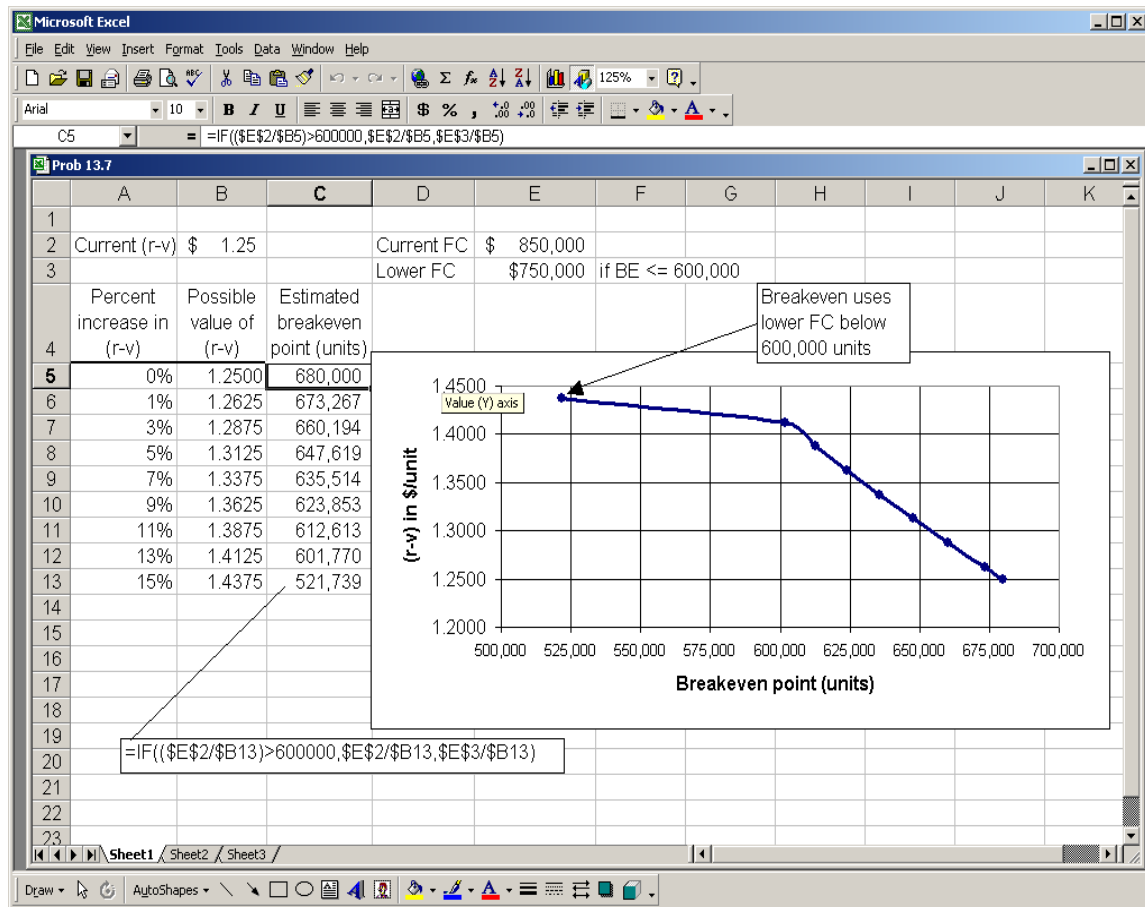
Average revenue required for the new product only is 60 cents per call lower.

13.7 Calculate $Q_{BE} = FC/(r-v)$ for $(r-v)$ increases of 1% through 15% and plot.



The breakeven point decreases linearly from 680,000 currently to 591,304 if a 15% increase in $(r-v)$ is experienced. If r and FC are constant, this means all the reduction must take place in a **lower variable cost per unit**.

13.8 Rework the spreadsheet above to include an IF statement for the computation of Q_{BE} for the reduced FC of \$750,000. The breakeven point falls substantially to 521,739 when the lower FC is in effect.



Note: To guarantee that the cell computations in column C correctly track when the breakeven point falls below 600,000, the same IF statement is used in all cells. With this feature, sensitivity analysis on the 600,000 estimate may also be performed.

13.9 Let x = gradient increase per year. Set revenue = cost.

$$[4000 + x(A/G, 12\%, 3)](33,000 - 21,000) = -200,000,000(A/P, 12\%, 3) + (0.20)(200,000,000)(A/F, 12\%, 3)$$

$$[4000 + x (0.9246)](12,000) = -200,000,000(0.41635) + 40,000,000(0.29635)$$

$$x = 2110 \text{ cars/year increase}$$

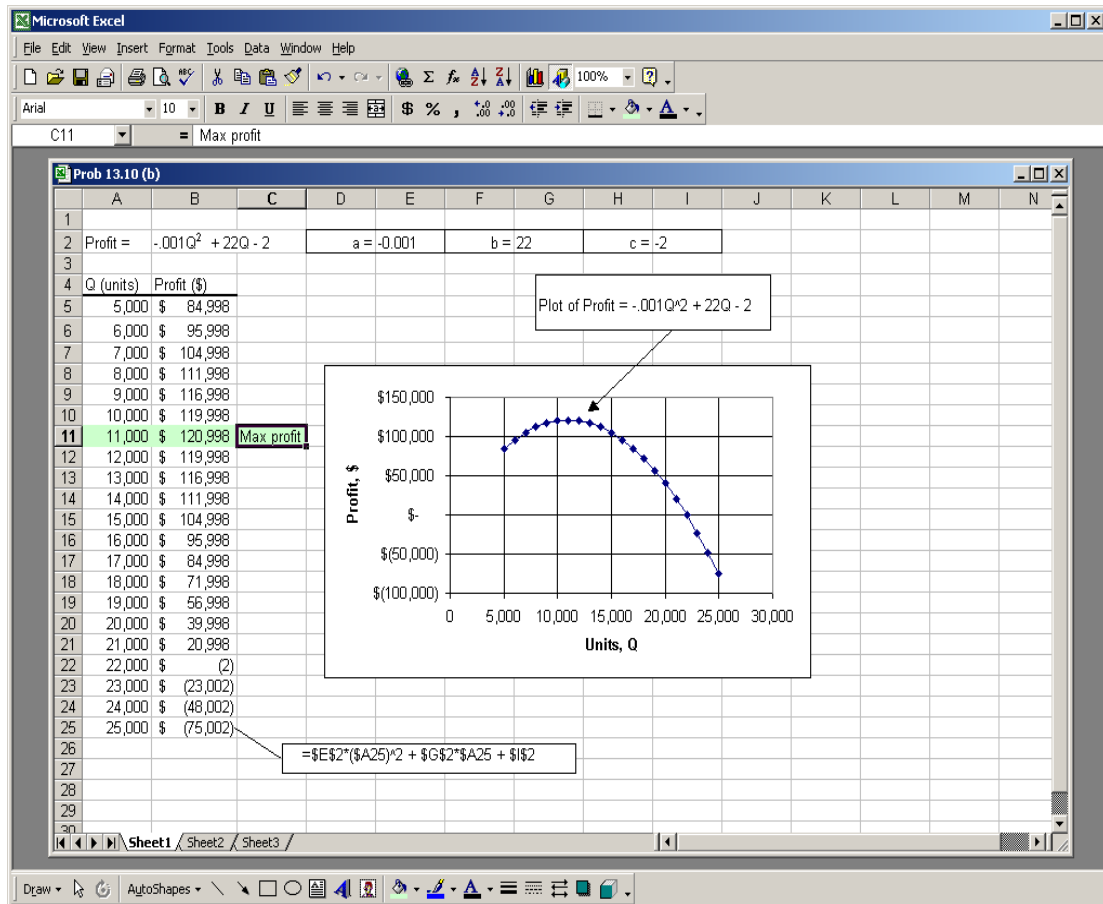
13.10 (a) Profit = $R - TC = 25Q - 0.001Q^2 - 3Q - 2$
 $= -0.001Q^2 + 22Q - 2$

Q	Profit (approximate)
5,000	\$ 85,000

10,000	120,000
11,000	121,000
15,000	105,000
20,000	40,000
25,000	-75,000

About 11,000 cases per year is breakeven with profit of \$121,000.

- (b) Develop the Excel graph for Q vs Profit $= -0.001Q^2 + 22Q - 2$ that indicates a max profit of \$120,998 at $Q = 11,000$ units.



- (c) In general, Profit $= R - TC = aQ^2 + bQ + c$

The a , b and c are constants. Take the first derivative, set equal to 0, and solve.

$$Q_{\max} = -b/2a$$

Substitute into the profit relation.

$$Profit_{\max} = (-b^2/4a) + c$$

Here, $Q_{\max} = 22/2(0.001)$
 $= 11,000$ cases per year

$$\text{Profit}_{\max} = [-(22)^2/4(-0.001)] - 2$$

$$= \$120,998 \text{ per year}$$

13.11 $FC = \$305,000$ $v = \$5500/\text{unit}$

(a) $\text{Profit} = (r - v)Q - FC$

$$0 = (r - 5500)5000 - 305,000$$

$$(r - 5500) = 305,000 / 5000$$

$$r = 61 + 5500$$

$$= \$5561 \text{ per unit}$$

(b) $\text{Profit} = (r - v)Q - FC$

$$500,000 = (r - 5500)8000 - 305,000$$

$$(r - 5500) = (500,000 + 305,000) / 8000$$

$$r = \$5601 \text{ per unit}$$

13.12 Let x = ads per year

$$-12,000(A/P, 8\%, 3) - 45,000 + 2000(A/F, 8\%, 3) - 8x = -20x$$

$$-12,000(0.38803) - 45,000 + 2000(0.30803) = -12x$$

$$-49,040 = -12x$$

$$x = 4087 \text{ ads per year}$$

At 4000 ads per year, select the outsource option at \$20 per ad for a total cost of \$80,000 versus the inhouse option cost of $\$49,040 + 8(4000) = \$81,040$.

13.13 Let n = number of months

$$-15,000(A/P, 0.5\%, n) - 80 = -1000$$

$$-15,000(A/P, 0.5\%, n) = -920$$

$$(A/P, 0.5\%, n) = 0.0613$$

n is approximately 17 months

13.14 Let x = hours per year

$$-800(A/P, 10\%, 3) - (300/2000)x - 1.0x = -1,900(A/P, 10\%, 5) - (700/8000)x - 1.0x$$

$$-800(0.40211) - 0.15x - 1.0x = -1,900(0.2638) - 0.0875x - 1.0x$$

$$0.0625x = 179.532$$

$$x = 2873 \text{ hours per year}$$

- 13.15 Set $AW_1 = AW_2$ where P_2 = first cost of Proposal 2. The final term in AW_2 removes the repainting cost in year 8.

$$-250,000(A/P, 12\%, 4) - 3,000 = -P_2(A/P, 12\%, 8) - 3,000(A/F, 12\%, 2) + 3,000(A/F, 12\%, 8)$$

$$-250,000(0.32923) - 3,000 = -P_2(0.2013) - 3,000(0.4717) + 3,000(0.0813)$$

$$-85,307.50 = -P_2(0.2013) - 1171.20$$

$$-84,136.30 = -P_2(0.2013)$$

$$P_2 = \$417,965$$

- 13.16 Let x = production in year 4. Determine variable costs in year 4 and set the cost relations equal. The 10% interest rate is not needed.

$$-400,000 - 86x = -750,000 - 62x$$

$$24x = 350,000$$

$$x = 14,584 \text{ units}$$

- 13.17 (a) Let x = breakeven days per year. Use annual worth analysis.

$$-125,000(A/P, 12\%, 8) + 5,000(A/F, 12\%, 8) - 2,000 - 40x = -45(125 + 20x)$$

$$-125,000(0.2013) + 5,000(0.0813) - 2,000 - 40x = -5625 - 900x$$

$$-26,756 - 40x = -5625 - 900x$$

$$-21,131 = -860x$$

$$x = 24.6 \text{ days per year}$$

- (b) Since $75 > 24.6$ days, select the buy. Annual cost is

$$-26,756 - 40(75) = \$-29,756$$

- 13.18 Let FC_B = fixed cost for B. Set total cost relations equal at 2000 units per year.

$$\text{Variable cost for B} = 2000/200 = \$10/\text{unit}$$

$$40,000 + 60(2000 \text{ units}) = FC_B + 10(2000 \text{ units})$$

$$FC_B = \$140,000 \text{ per year}$$

- 13.19 (a) Let x = days per year to pump the lagoon. Set the AW relations equal.

$$-800(A/P, 10\%, 8) - 300x = -1600(A/P, 10\%, 10) - 3x - 12(8200)(A/P, 10\%, 10)$$

$$\begin{aligned}
 -800(0.18744) - 300x &= -1600(0.16275) - 3x - 98,400(0.16275) \\
 -149.95 - 300x &= -16275 - 3x \\
 297x &= 16125.05
 \end{aligned}$$

$$x = 54.3 \text{ days per year}$$

(b) If the lagoon is pumped 52 times per year and P = cost of pipeline, the breakeven equation in (a) becomes:

$$-800(0.18744) - 300(52) = -1600(0.16275) - 3(52) + P(0.16275)$$

$$-15,750 = -416.4 + 0.16275P$$

$$P = \$-94,216$$

13.20 (a) Excel spreadsheet, SOLVER entries, and solution for $P = -\$417,964$ are below.

The screenshot shows an Excel spreadsheet with the following data:

	A	B	C	D	E	F
1		MARR =	12%			
2						
3	Proposal	#1	#2			
4	Initial cost	-\$250,000	\$0			
5	Annual cost	-\$3,000				
6	2-year cost		-\$3,000			
7	Life, years	4	8			
8						
9		Cash flows				
10	Year	Prop 1	Prop 2			
11	0	\$ (250,000)	\$ -			
12	1	\$ (3,000)	\$ -			
13	2	\$ (3,000)	\$ (3,000)			
14	3	\$ (3,000)	\$ -			
15	4	\$ (3,000)	\$ (3,000)			
16	5		\$ -			
17	6		\$ (3,000)			
18	7		\$ -			
19	8		\$ -			
20	AW	\$85,308.61	\$1,171.19			
21						

Annotations in the image:

- "Initial cost estimate is needed" points to cell C4 (\$0).
- "Changing cell" points to cell C11 (\$ -).
- "Target cell" points to cell C20 (\$1,171.19).

The Solver Parameters dialog box is configured as follows:

- Set Target Cell:** \$C\$20
- Equal To:** ☒ Max ☐ Min ☐ Value of: 85308.61
- By Changing Cells:** \$C\$11
- Subject to the Constraints:** (Empty list)
- Buttons:** Solve, Close, Options, Reset All, Help, Add, Change, Delete, Guess.

13.20 (a) (cont)

Microsoft Excel - Prob 13.20(a) - solution						
File Edit View Insert Format Tools Data Window Help						
14	B					
C20		=PMT(\$C\$1,\$C\$7,(NPV(\$C\$1,C12:C19)+C11))				
	A	B	C	D	E	F
1		MARR = 12%				
2						
3	Proposal	#1	#2			
4	Initial cost	-\$250,000	\$0			
5	Annual cost	-\$3,000				
6	2-year cost		-\$3,000			
7	Life, years	4	8			
8						
9		Cash flows				
10	Year	Prop 1	Prop 2			
11	0	\$ (250,000)	\$ (417,964)			
12	1	\$ (3,000)	\$ -			
13	2	\$ (3,000)	\$ (3,000)			
14	3	\$ (3,000)	\$ -			
15	4	\$ (3,000)	\$ (3,000)			
16	5		\$ -			
17	6		\$ (3,000)			
18	7		\$ -			
19	8		\$ -			
20	AW	\$85,308.61	\$85,308.61			
21						

Solution with
P = \$-417,964

- 13.20 (b) Set cell C2 to $-\$400,000$. The changing cells in SOLVER are B12 through B15. If no constraints are placed on the annual cash flows for proposal 1, the SOLVER solution has positive annual 'costs' in years 2, 3 and 4, which are not acceptable. The answer is 'no'.

	A	B	C	D	E	F	G	H	I	J	K	L
1		MARR = 12%										
2												
3	Proposal	#1	#2									
4	Initial cost	-\$250,000	-\$400,000									
5	Annual cost	-\$3,000										
6	2-year cost		-\$3,000									
7	Life, years	4	8									
8												
9		Cash flows										
10	Year	Prop 1	Prop 2									
11	0	\$ (250,000)	\$ (400,000)									
12	1	(\$3,000)	\$ -									
13	2	\$1,179	\$ (3,000)									
14	3	\$731	\$ -									
15	4	\$332	\$ (3,000)									
16	5		\$ -									
17	6		\$ (3,000)									
18	7		\$ -									
19	8		\$ -									
20	AW	\$81,692.32	\$81,692.32									
21												

If constraints are made using SOLVER for cells B12 through B15 to not become positive, SOLVER finds no solution for break even. The answer, again, is 'no'.

Solver Parameters

Set Target Cell:

Equal To: ☐ Max ☐ Min ☒ Value of:

By Changing Cells:

Subject to the Constraints:

Buttons: Solve, Close, Options, Reset All, Help, Add, Change, Delete, Guess.

- 13.21 Let x = yards per year to breakeven
 (a) Solution by hand

$$\begin{aligned}
 & -40,000(A/P, 8\%, 10) - 2,000 - (30/2500)x = - [6(14)/2500]x \\
 & -40,000(0.14903) - 2,000 - 0.012x = -0.0336x \\
 & -7961.20 = -0.0216x \\
 & x = 368,574 \text{ yards per year}
 \end{aligned}$$

(b) Solution by computer

There are many Excel set-ups to work the problem. One is: Enter the parameters for each alternative, including some number of yards per year as a guess. Use SOLVER to force the breakeven equation (target cell D15) to equal 0, with a constraint in SOLVER that total yardage be the same for both alternatives (cell B9 = C9).

	A	B	C	D
1	MARR	8%	Human: rate/hr	\$ 14
2				
3	Alternatives	Machine (M)	Human (H)	
4	Cost, \$	-40,000		
5	Life, years	10		
6	AOC, \$/yr	-2000		
7	Cut rate/hr	2500	2500	
8	Cost/hr, \$	30	84	
9	Yards/yr	368573	368573	
10				
11	AW of machine	\$ 7,961		
12	Yardage cost, \$	\$ 4,423	\$ 12,384	
13	Total cost/yr	\$ 12,384	\$ 12,384	
14				
15	To break even, TC(M) - TC(H) = 0			\$0
16				
17				

Solver Parameters

Set Target Cell:

Equal To: ☐ Max ☐ Min ☒ Value of:

By Changing Cells:

Subject to the Constraints:

Buttons: Solve, Close, Options, Reset All, Help

13.22 Put in new values, use the Same SOLVER screen and obtain $B_E = 268,113$ yards/year.

Microsoft Excel - Prob 13.22

File Edit View Insert Format Tools Data Window Help

Arial 10 B

D15 = =\$B\$13-\$C\$13

	A	B	C	D	E	F
1	MARR	6%	Human: rate/hr	\$ 25		
2						
3	Alternatives	Machine (M)	Human (H)			
4	Cost, \$	-80,000				
5	Life, years	10				
6	AOC, \$/yr	-2000				
7	Cut rate/hr	2500	2500			
8	Cost/hr, \$	30	150			
9	Yards/yr	268,113	268,113			
10						
11	AW of machine	\$ 12,869				
12	Yardage cost, \$	\$ 3,217	\$ 16,087			
13	Total cost/yr	\$ 16,087	\$ 16,087			
14						
15	To break even, TC(M) - TC(H) = 0			\$0		
16						
17						

Sheet1 Sheet2 Sheet3

Since now the annual yardage rate of 300,000 > 268,113, the lower variable cost alternative of the machine should be selected.

13.23 (a) Let n = number of years. Develop the relation

$$AW_{\text{own}} + AW_{\text{lease}} + AW_{\text{sell}} = 0$$

$$-(100,000 + 12,000)(A/P, 8\%, n) - 3800 - 2500 - [1000(P/F, 8\%, k)](A/P, 8\%, n) + 12,000 + (60 + 1.5n)(2,500)(A/F, 8\%, n) = 0$$

where $k = 6, 12, 18, \dots$, and $k \leq n$.

Use trial and error to determine the breakeven n value.

$$n = 14: -112,000(0.12130) + 5700 - [1000(0.6302 + 0.3971)](0.12130) + [60 + 1.5(14)](2,500)(0.04130) \neq 0$$

$$-13,586 + 5700 - 125 + 8363 = \$+352 > 0$$

13.23 (cont)

$$n = 16: -112,000(0.11298) + 5700 - [1000(0.6302 + 0.3971)](0.11298) + [60 + 1.5(16)](2,500)(0.03298) \neq 0$$

$$-12,654 + 5700 - 116 + 6926 = \$-144 < 0$$

By interpolation, $n = 15.42$ years

$$\begin{aligned} \text{Selling price} &= [60 + 1.5(15.42)] (2,500) \\ &= \$207,825 \end{aligned}$$

- (b) Enter the cash flows and carefully develop the PW relations for each column.
Breakeven is between 15 and 16 years. Selling price is estimated to be between \$206,250 and \$210,000. Linear interpolation can be used as in the manual trial and error method above.

Microsoft Excel - Prob 13.23(b)

	A	B	C	D	E	F	G	H	I	J
1			MARR	8%						
2										
3				PW own + lease	Total PW	Estimated		Total		
4	Year	Own	Lease	only	own + lease	selling price	PW sell	PW		
5	0	-112000								
6	1	-6300	12000	\$ 5,278	\$ (106,722)	\$ 153,750	\$142,361	\$ 35,639		
7	2	-6300	12000	\$ 10,165	\$ (101,835)	\$ 157,500	\$135,031	\$ 33,195		
8	3	-6300	12000	\$ 14,689	\$ (97,311)	\$ 161,250	\$128,005	\$ 30,695		
9	4	-6300	12000	\$ 18,879	\$ (93,121)	\$ 165,000	\$121,280	\$ 28,159		
10	5	-6300	12000	\$ 22,758	\$ (89,242)	\$ 168,750	\$114,848	\$ 25,607		
11	6	-7300	12000	\$ 25,720	\$ (86,280)	\$ 172,500	\$108,704	\$ 22,425		
12	7	-6300	12000	\$ 29,046	\$ (82,954)	\$ 176,250	\$102,840	\$ 19,886		
13	8	-6300	12000	\$ 32,126	\$ (79,874)	\$ 180,000	\$97,248	\$ 17,374		
14	9	-6300	12000	\$ 34,977	\$ (77,023)	\$ 183,750	\$91,921	\$ 14,898		
15	10	-6300	12000	\$ 37,617	\$ (74,383)	\$ 187,500	\$86,849	\$ 12,466		
16	11	-6300	12000	\$ 40,062	\$ (71,938)	\$ 191,250	\$82,024	\$ 10,086		
17	12	-7300	12000	\$ 41,928	\$ (70,072)	\$ 195,000	\$77,437	\$ 7,366		
18	13	-6300	12000	\$ 44,024	\$ (67,976)	\$ 198,750	\$73,080	\$ 5,104		
19	14	-6300	12000	\$ 45,965	\$ (66,035)	\$ 202,500	\$68,943	\$ 2,908		
20	15	-6300	12000	\$ 47,762	\$ (64,238)	\$ 206,250	\$65,019	\$ 780		
21	16	-6300	12000	\$ 49,426	\$ (62,574)	\$ 210,000	\$61,297	\$ (1,277)		
22	17	-6300	12000	\$ 50,966	\$ (61,034)	\$ 213,750	\$57,770	\$ (3,264)		
23	18	-7300	12000	\$ 52,142	\$ (59,858)	\$ 217,500	\$54,429	\$ (5,429)		
24	19	-6300	12000	\$ 53,463	\$ (58,537)	\$ 221,250	\$51,266	\$ (7,271)		
25	20	-6300	12000	\$ 54,686	\$ (57,314)	\$ 225,000	\$48,273	\$ (9,041)		
26										
27										
28										
29										
30										

Formulas shown in the image:

- Cell B25: $=NPV(\$D\$1, \$B\$6: \$B\$25) + NPV(\$D\$1, \$C\$6: \$C\$25)$
- Cell D25: $=D25 + B\$5$
- Cell F25: $=2500*(60 + 1.5*A25)$
- Cell H25: $=PV(\$D\$1, A25, , F25)$
- Cell I25: $=E25 + G25$

Breakeven occurs here

13.24 Let x = number of samples per year. Set AW values for complete and partial labs equal to the complete outsource cost.

- (a) Complete lab option
 $-50,000(A/P, 10\%, 6) - 26,000 - 10x = -120x$
 $-50,000(0.22961) - 26,000 = -110x$

$$x = 341 \text{ samples per year}$$

(b) Partial lab option

$$-35,000(A/P, 10\%, 6) - 10,000 - 3x - 40x = -120x$$

$$-35,000(0.22961) - 10,000 = -77x$$

$$x = 234 \text{ samples per year}$$

(c) Equate AW of complete and partial labs

$$-50,000(A/P, 10\%, 6) - 26,000 - 10x = -35,000(A/P, 10\%, 6) - 10,000 - 3x - 40x$$

$$-50,000(0.22961) - 26,000 - 10x = -35,000(0.22961) - 10,000 - 43x$$

$$33x = 19,444$$

$$x = 589 \text{ samples per year}$$

Ranges for the lowest total cost are:

$0 < x \leq 234$	select outsource
$234 < x \leq 589$	select partial lab
$589 < x$	select complete lab

(d) At 300 samples per year, the partial lab option is the best economically at
 $TC = \$30,936$.

13.25 Let P = initial cost of plastic lining. Use AW analysis.

(a) by hand: $-8,000(A/P, 4\%, 6) - 1000(P/F, 4\%, 3)(A/P, 4\%, 6) = -P(A/P, 4\%, 15)$
 $-8,000(0.19076) - 1000(0.8890)(0.19076) = -P(0.08994)$
 $-1695.66 = -P(0.08994)$
 $P = \$18,853$

(b) by computer: Enter cash flows and set SOLVER to find the initial cost of plastic liner alternative (Cell C4 here).

The Excel spreadsheet shows the following data:

Year	Bituminous	Plastic
0	-\$8,000	-\$18,857
1	\$0	\$0
2	\$0	\$0
3	-\$1,000	\$0
4	\$0	\$0
5	\$0	\$0
6	\$0	\$0
7		\$0
8		\$0
9		\$0
10		\$0
11		\$0
12		\$0
13		\$0
14		\$0
15		\$0
PW	-\$8,889	-\$18,857
AW	-\$1,696	-\$1,696

The Solver Parameters dialog box is configured as follows:

- Set Target Cell: $\$C\22
- Equal To: ☒ Value of: -1696
- By Changing Cells: $\$C\4
- Subject to the Constraints: (empty)

Buttons: Solve, Close, Options, Add, Change, Delete, Reset All, Help.

Changing cell to make the AW values equal

13.26 (a) By hand: Let P = first cost of sandblasting. Equate the PW of painting each 4

years to PW of sandblasting each 10 years, up to a total of 38 years for each option.

PW of painting

$$\begin{aligned}
 PW_p &= -2,800 - 3,360(P/F, 10\%, 4) - 4,032(P/F, 10\%, 8) - 4,838(P/F, 10\%, 12) - \\
 &\quad 5,806(P/F, 10\%, 16) - 6,967(P/F, 10\%, 20) - 8,361(P/F, 10\%, 24) - \\
 &\quad 10,033(P/F, 10\%, 28) - 12,039(P/F, 10\%, 32) - 14,447(P/F, 10\%, 36) \\
 &= -2,800 - 3,360(0.6830) - 4,032(0.4665) - 4,838(0.3186) \\
 &\quad - 5,806(0.2176) - 6,967(0.1486) - 8,361(0.1015) - 10,033(0.0693) \\
 &\quad - 12,039(0.0474) - 14,447(0.0323) \\
 &= \$-13,397
 \end{aligned}$$

PW of sandblasting

$$\begin{aligned}
 PW_s &= -P - 1.4P(P/F, 10\%, 10) - 1.96P(P/F, 10\%, 20) - 2.74P(P/F, 10\%, 30) \\
 &\quad - P[1 + 1.4(0.3855) + 1.96(0.1486) + 2.74(0.0573)] \\
 &= -1.988P
 \end{aligned}$$

Equate the PW relations.

$$\begin{aligned}
 -13,397 &= -1.988P \\
 P &= \$6,739
 \end{aligned}$$

- (b) By computer: Enter the periodic costs. Enter 0 for the P of the sandblasting option. Use SOLVER to find breakeven at P = -\$6739 (cell C6). (Note that many of the year entries are hidden in the Excel image below.)

The screenshot shows an Excel spreadsheet titled "Prob 13.26" with the following data:

Year	Paint	Sandblast
0	-\$2,800	-\$6,739
1	\$0	\$0
2	\$0	\$0
8	-\$4,032	\$0
9	\$0	\$0
10	\$0	-\$9,434
11	\$0	\$0
12	-\$4,838	\$0
20	-\$6,967	-\$13,208
21	\$0	\$0
22	\$0	\$0
28	-\$10,033	\$0
29	\$0	\$0
30	\$0	-\$18,491
31	\$0	\$0
36	-\$14,447	\$0
37	\$0	\$0
38	\$0	\$0

The "Solver Parameters" dialog box is configured as follows:

- Set Target Cell: $\$C\5
- Equal To: ☐ Max ☐ Min ☒ Value of: -13399
- By Changing Cells: $\$C\6
- Subject to the Constraints: (empty)

(c) Change cell C2 to 30% and then 20% and re-SOLVER to get:

30%: $P = -\$7133$

20%: $P = -\$7546$

Case Study Solution

1. Savings = $40 \text{ hp} * 0.75 \text{ kw/hp} * 0.06 \text{ \$/kwh} * 24 \text{ hr/day} * 30.5 \text{ days/mo} \div 0.90$
= \$1464/month
2. A decrease in the efficiency of the aerator motor renders the selected alternative of “sludge recirculation only” *more* attractive, because the cost of aeration would be higher, and, therefore the net savings from its discontinuation would be greater.
3. If the cost of lime increased by 50%, the lime costs for “sludge recirculation only” and “neither aeration nor sludge recirculation” would increase by 50% to \$393 and \$2070, respectively. Therefore, the cost difference would *increase*.
4. If the efficiency of the sludge recirculation pump decreased from 90% to 70%, the net savings between alternatives 3 and 4 would *decrease*. This is because the \$262 saved by not recirculating with a 90% efficient pump would increase to a monthly savings of \$336 by not recirculating with a 70% efficient pump.
5. If hardness removal were discontinued, the extra cost for its removal (column 4 in Table 13-1) would be zero for all alternatives. The favored alternative under this scenario would be alternative 4 (neither aeration nor sludge recirculation) with a total savings of $\$2,471 - 469 = \2002 per month.
6. If the cost of electricity decreased to 4¢/kwh, the aeration and sludge recirculation monthly costs would be \$976 and \$122, respectively. The net savings for alternative 2 would then be \$-1727, for alternative 3 would be \$-131, and for alternative four - \$751---all losses. Therefore, the best alternative would be number 1, continuation of the normal operating condition.
7. (a) For alternatives 1 and 2 to breakeven, the total savings would have to be equal to the total extra cost of \$1,849. Thus,

$$1,849 / 30.5 = (5)(0.75)(x)(24) / 0.90$$
$$x = 60.6 \text{ cents per kwh}$$

(b) $1107 / 30.5 = (40)(0.75)(x)(24) / 0.90$

$$x = 4.5 \text{ cents per kwh}$$

(c) $1,849 / 30.5 = (5)(0.75)(x)(24) / 0.90 + (40)(0.75)(x)(24) / 0.90$

$$x = 6.7 \text{ cents per kwh}$$