

## Chapter 2

### Factors: How Time and Interest Affect Money

#### Solutions to Problems

2.1 1.  $(F/P, 8\%, 25) = 6.8485$ ; 2.  $(P/A, 3\%, 8) = 7.0197$ ; 3.  $(P/G, 9\%, 20) = 61.7770$ ;  
4.  $(F/A, 15\%, 18) = 75.8364$ ; 5.  $(A/P, 30\%, 15) = 0.30598$

2.2  $P = 140,000(F/P, 7\%, 4)$   
 $= 140,000(1.3108)$   
 $= \$183,512$

2.3  $F = 200,000(F/P, 10\%, 3)$   
 $= 200,000(1.3310)$   
 $= \$266,200$

2.4  $P = 600,000(P/F, 12\%, 4)$   
 $= 600,000(0.6355)$   
 $= \$381,300$

2.5 (a)  $A = 225,000(A/P, 15\%, 4)$   
 $= 225,000(0.35027)$   
 $= \$78,811$

(b) Recall amount  $= 78,811/0.10$   
 $= \$788,110$  per year

2.6  $F = 150,000(F/P, 18\%, 7)$   
 $= 150,000(3.1855)$   
 $= \$477,825$

2.7  $P = 75(P/F, 18\%, 2)$   
 $= 75(0.7182)$   
 $= \$53.865$  million

2.8  $P = 100,000((P/F, 12\%, 2)$   
 $= 100,000(0.7972)$   
 $= \$79,720$

2.9  $F = 1,700,000(F/P, 18\%, 1)$   
 $= 1,700,000(1.18)$   
 $= \$2,006,000$

$$\begin{aligned}
 2.10 \quad P &= 162,000(P/F, 12\%, 6) \\
 &= 162,000(0.5066) \\
 &= \$82,069
 \end{aligned}$$

$$\begin{aligned}
 2.11 \quad P &= 125,000(P/F, 14\%, 5) \\
 &= 125,000(0.5149) \\
 &= \$ 64,925
 \end{aligned}$$

$$\begin{aligned}
 2.12 \quad P &= 9000(P/F, 10\%, 2) + 8000(P/F, 10\%, 3) + 5000(P/F, 10\%, 5) \\
 &= 9000(0.8264) + 8000(0.7513) + 5000(0.6209) \\
 &= \$16,553
 \end{aligned}$$

$$\begin{aligned}
 2.13 \quad P &= 1,250,000(0.10)(P/F, 8\%, 2) + 500,000(0.10)(P/F, 8\%, 5) \\
 &= 125,000(0.8573) + 50,000(0.6806) \\
 &= \$141,193
 \end{aligned}$$

$$\begin{aligned}
 2.14 \quad F &= 65,000(F/P, 4\%, 5) \\
 &= 65,000(1.2167) \\
 &= \$79,086
 \end{aligned}$$

$$\begin{aligned}
 2.15 \quad P &= 75,000(P/A, 20\%, 3) \\
 &= 75,000(2.1065) \\
 &= \$157,988
 \end{aligned}$$

$$\begin{aligned}
 2.16 \quad A &= 1.8(A/P, 12\%, 6) \\
 &= 1.8(0.24323) \\
 &= \$437,814
 \end{aligned}$$

$$\begin{aligned}
 2.17 \quad A &= 3.4(A/P, 20\%, 8) \\
 &= 3.4(0.26061) \\
 &= \$886,074
 \end{aligned}$$

$$\begin{aligned}
 2.18 \quad P &= (280,000 - 90,000)(P/A, 10\%, 5) \\
 &= 190,000(3.7908) \\
 &= \$720,252
 \end{aligned}$$

$$\begin{aligned}
 2.19 \quad P &= 75,000(P/A, 15\%, 5) \\
 &= 75,000(3.3522) \\
 &= \$251,415
 \end{aligned}$$

$$\begin{aligned}
 2.20 \quad F &= (458 - 360)(20,000)(0.90)(F/A, 8\%, 5) \\
 &= 1,764,000(5.8666) \\
 &= \$10,348,682
 \end{aligned}$$

$$\begin{aligned}
 2.21 \quad P &= 200,000(P/A, 10\%, 5) \\
 &= 200,000(3.7908) \\
 &= \$758,160
 \end{aligned}$$

$$\begin{aligned}
 2.22 \quad P &= 2000(P/A, 8\%, 35) \\
 &= 2000(11.6546) \\
 &= \$23,309
 \end{aligned}$$

$$\begin{aligned}
 2.23 \quad A &= 250,000(A/F, 9\%, 3) \\
 &= 250,000(0.30505) \\
 &= \$76,263
 \end{aligned}$$

$$\begin{aligned}
 2.24 \quad F &= (100,000 + 125,000)(F/A, 15\%, 3) \\
 &= 225,000(3.4725) \\
 &= \$781,313
 \end{aligned}$$

$$\begin{aligned}
 2.25 \quad (a) \quad 1. & \text{ Interpolate between } n = 32 \text{ and } n = 34: \\
 & 1/2 = x/0.0014 \\
 & x = 0.0007 \\
 & (P/F, 18\%, 33) = 0.0050 - 0.0007 \\
 & \quad = 0.0043
 \end{aligned}$$

$$\begin{aligned}
 & 2. \text{ Interpolate between } n = 50 \text{ and } n = 55: \\
 & 4/5 = x/0.0654 \\
 & x = 0.05232 \\
 & (A/G, 12\%, 54) = 8.1597 + 0.05232 \\
 & \quad = 8.2120
 \end{aligned}$$

$$\begin{aligned}
 (b) \quad 1. & (P/F, 18\%, 33) = 1/(1+0.18)^{33} \\
 & \quad = 0.0042
 \end{aligned}$$

$$\begin{aligned}
 2. & (A/G, 12\%, 54) = \{(1/0.12) - 54/[(1+0.12)^{54} - 1]\} \\
 & \quad = 8.2143
 \end{aligned}$$

$$\begin{aligned}
 2.26 \quad (a) \quad 1. & \text{ Interpolate between } i = 18\% \text{ and } i = 20\% \text{ at } n = 20: \\
 & 1/2 = x/40.06 \\
 & x = 20.03 \\
 & (F/A, 19\%, 20) = 146.6280 + 20.03 \\
 & \quad = 166.658
 \end{aligned}$$

$$\begin{aligned}
 2. & \text{ Interpolate between } i = 25\% \text{ and } i = 30\% \text{ at } n = 15: \\
 & 1/5 = x/0.5911 \\
 & x = 0.11822 \\
 & (P/A, 26\%, 15) = 3.8593 - 0.11822 \\
 & \quad = 3.7411
 \end{aligned}$$

$$(b) \quad 1. (F/A, 19\%, 20) = [(1 + 0.19)^{20} - 0.19]/0.19 \\ = 169.6811$$

$$2. (P/A, 26\%, 15) = [(1 + 0.26)^{15} - 1]/[0.26(1 + 0.26)^{15}] \\ = 3.7261$$

$$2.27 \quad (a) G = \$200 \quad (b) CF_8 = \$1600 \quad (c) n = 10$$

$$2.28 \quad (a) G = \$5 \text{ million} \quad (b) CF_6 = \$6030 \text{ million} \quad (c) n = 12$$

$$2.29 \quad (a) G = \$100 \quad (b) CF_5 = 900 - 100(5) = \$400$$

$$2.30 \quad 300,000 = A + 10,000(A/G, 10\%, 5) \\ 300,000 = A + 10,000(1.8101) \\ A = \$281,899$$

$$2.31 \quad (a) CF_3 = 280,000 - 2(50,000) \\ = \$180,000 \\ (b) A = 280,000 - 50,000(A/G, 12\%, 5) \\ = 280,000 - 50,000(1.7746) \\ = \$191,270$$

$$2.32 \quad (a) CF_3 = 4000 + 2(1000) \\ = \$6000 \\ (b) P = 4000(P/A, 10\%, 5) + 1000(P/G, 10\%, 5) \\ = 4000(3.7908) + 1000(6.8618) \\ = \$22,025$$

$$2.33 \quad P = 150,000(P/A, 15\%, 8) + 10,000(P/G, 15\%, 8) \\ = 150,000(4.4873) + 10,000(12.4807) \\ = \$797,902$$

$$2.34 \quad A = 14,000 + 1500(A/G, 12\%, 4) \\ = 14,000 + 1500(1.3589) \\ = \$16,038$$

$$2.35 \quad (a) \text{Cost} = 2000/0.2 \\ = \$10,000 \\ (b) A = 2000 + 250(A/G, 18\%, 5) \\ = 2000 + 250(1.6728) \\ = \$2418$$

2.36 Convert future to present and then solve for G using P/G factor:

$$\begin{aligned}6000(P/F, 15\%, 4) &= 2000(P/A, 15\%, 4) - G(P/G, 15\%, 4) \\6000(0.5718) &= 2000(2.8550) - G(3.7864) \\G &= \$601.94\end{aligned}$$

2.37  $50 = 6(P/A, 12\%, 6) + G(P/G, 12\%, 6)$

$$50 = 6(4.1114) + G(8.9302)$$

$$G = \$2,836,622$$

2.38  $A = [4 + 0.5(A/G, 16\%, 5)] - [1 - 0.1(A/G, 16\%, 5)]$

$$= [4 + 0.5(1.7060)] - [1 - 0.1(1.7060)]$$

$$= \$4,023,600$$

2.39 For n = 1:  $\{1 - [(1+0.04)^1/(1+0.10)^1]\}/(0.10 - 0.04) = 0.9091$

For n = 2:  $\{1 - [(1+0.04)^2/(1+0.10)^2]\}/(0.10 - 0.04) = 1.7686$

For n = 3:  $\{1 - [(1+0.04)^3/(1+0.10)^3]\}/(0.10 - 0.04) = 2.5812$

2.40 For g = i,  $P = 60,000(0.1)[15/(1 + 0.04)]$

$$= \$86,538$$

2.41  $P = 25,000\{1 - [(1+0.06)^3/(1+0.15)^3]\}/(0.15 - 0.06)$

$$= \$60,247$$

2.42 Find P and then convert to A.

$$P = 5,000,000(0.01)\{1 - [(1+0.20)^5/(1+0.10)^5]\}/(0.10 - 0.20)$$

$$= 50,000\{5.4505\}$$

$$= \$272,525$$

$$A = 272,525(A/P, 10\%, 5)$$

$$= 272,525(0.26380)$$

$$= \$71,892$$

2.43 Find P and then convert to F.

$$P = 2000\{1 - [(1+0.10)^7/(1+0.15)^7]\}/(0.15 - 0.10)$$

$$= 2000(5.3481)$$

$$= \$10,696$$

$$F = 10,696(F/P, 15\%, 7)$$

$$= 10,696(2.6600)$$

$$= \$28,452$$

2.44 First convert future worth to P, then use  $P_g$  equation to find A.

$$P = 80,000(P/F, 15\%, 10)$$

$$= 80,000(0.2472)$$

$$= \$19,776$$

$$19,776 = A \{ 1 - [(1+0.09)^{10}/(1+0.15)^{10}] \} / (0.15 - 0.09)$$

$$19,776 = A \{ 6.9137 \}$$

$$A = \$2860$$

2.45 Find A in year 1 and then find next value.

$$900,000 = A \{ 1 - [(1+0.05)^5/(1+0.15)^5] \} / (0.15 - 0.05)$$

$$900,000 = A \{ 3.6546 \}$$

$$A = \$246,263 \text{ in year 1}$$

$$\text{Cost in year 2} = 246,263(1.05)$$

$$= \$258,576$$

2.46  $g = i$ :  $P = 1000[20/(1 + 0.10)]$

$$= 1000[18.1818]$$

$$= \$18,182$$

2.47 Find P and then convert to F.

$$P = 3000 \{ 1 - [(1+0.05)^4/(1+0.08)^4] \} / (0.08 - 0.05)$$

$$= 3000 \{ 3.5522 \}$$

$$= \$10,657$$

$$F = 10,657(F/P, 8\%, 4)$$

$$= 10,657(1.3605)$$

$$= \$14,498$$

2.48 Decrease deposit in year 4 by 5% per year for three years to get back to year 1.

$$\text{First deposit} = 1250/(1 + 0.05)^3$$

$$= \$1079.80$$

2.49 Simple: Total interest =  $(0.12)(15) = 180\%$

Compound:  $1.8 = (1 + i)^{15}$

$$i = 4.0\%$$

2.50 Profit/year =  $6(3000)/0.05 = \$360,000$

$$1,200,000 = 360,000(P/A, i, 10)$$

$$(P/A, i, 10) = 3.3333$$

$$i = 27.3\% \text{ (Excel)}$$

2.51  $2,400,000 = 760,000(P/A, i, 5)$

$$(P/A, i, 5) = 3.15789$$

$$i = 17.6\% \text{ (Excel)}$$

2.52  $1,000,000 = 600,000(F/P, i, 5)$

$$(F/P, i, 5) = 1.6667$$

$$i = 10.8\% \text{ (Excel)}$$

$$2.53 \quad 125,000 = (520,000 - 470,000)(P/A, i, 4)$$

$$(P/A, i, 4) = 2.5000$$

$$i = 21.9\% \quad (\text{Excel})$$

$$2.54 \quad 400,000 = 320,000 + 50,000(A/G, i, 5)$$

$$(A/G, i, 5) = 1.6000$$

Interpolate between  $i = 22\%$  and  $i = 24\%$

$$i = 22.6\%$$

$$2.55 \quad 85,000 = 30,000(P/A, i, 5) + 8,000(P/G, i, 5)$$

Solve for  $i$  by trial and error or spreadsheet:

$$i = 38.9\% \quad (\text{Excel})$$

$$2.56 \quad 500,000 = 75,000(P/A, 10\%, n)$$

$$(P/A, 10\%, n) = 6.6667$$

From 10% table,  $n$  is between 11 and 12 years; therefore,  $n = 11$  years

$$2.57 \quad 160,000 = 30,000(P/A, 12\%, n)$$

$$(P/A, 12\%, n) = 5.3333$$

From 12% table,  $n$  is between 9 and 10 years; therefore,  $n = 10$  years

$$2.58 \quad 2,000,000 = 100,000(P/A, 4\%, n)$$

$$(P/A, 4\%, n) = 20.000$$

From 4% table,  $n$  is between 40 and 45 years; by spreadsheet,  $42 > n > 41$   
Therefore,  $n = 41$  years

$$2.59 \quad 1,500,000 = 3,000,000(P/F, 20\%, n)$$

$$(P/F, 20\%, n) = 0.5000$$

From 20% table,  $n$  is between 3 and 4 years; therefore,  $n = 4$  years

$$2.60 \quad 100,000 = 1,600,000(P/F, 18\%, n)$$

$$(P/F, 18\%, n) = 0.0625$$

From 18% table,  $n$  is between 16 and 17 years; therefore,  $n = 17$  years

$$2.61 \quad 10A = A(F/A, 10\%, n)$$

$$(F/A, 10\%, n) = 10.000$$

From 10% table,  $n$  is between 7 and 8 years; therefore,  $n = 8$  years

2.62  $1,000,000 = 10,000\{1 - [(1+0.10)^n/(1+0.07)^n]\}/(0.07 - 0.10)$   
 By trial and error, n = is between 50 and 51; therefore, n = 51 years

2.63  $12,000 = 3000 + 2000(A/G, 10\%, n)$   
 $(A/G, 10\%, n) = 4.5000$

From 10% table, n is between 12 and 13 years; therefore, n = 13 years

## FE Review Solutions

2.64  $P = 61,000(P/F, 6\%, 4)$   
 $= 61,000(0.7921)$   
 $= \$48,318$   
 Answer is (c)

2.65  $160 = 235(P/F, i, 5)$   
 $(P/F, i, 5) = 0.6809$   
 From tables, i = 8%  
 Answer is (c)

2.66  $23,632 = 3000\{1 - [(1+0.04)^n/(1+0.06)^n]\}/(0.06-0.04)$   
 $[(23,632*0.02)/3000]-1 = (0.98113)^n$   
 $\log 0.84245 = n\log 0.98113$   
 $n = 9$   
 Answer is (b)

2.67  $109.355 = 7(P/A, i, 25)$   
 $(P/A, i, 25) = 15.6221$   
 From tables, i = 4%  
 Answer is (a)

2.68  $A = 2,800,000(A/F, 6\%, 10)$   
 $= \$212,436$   
 Answer is (d)

2.69  $A = 10,000,000((A/P, 15\%, 7)$   
 $= \$2,403,600$   
 Answer is (a)

2.70  $P = 8000(P/A, 10\%, 10) + 500(P/G, 10\%, 10)$   
 $= 8000(6.1446) + 500(22.8913)$   
 $= \$60,602.45$   
 Answer is (a)

$$\begin{aligned}
 2.71 \quad F &= 50,000(F/P, 18\%, 7) \\
 &= 50,000(3.1855) \\
 &= \$159,275
 \end{aligned}$$

Answer is (b)

$$\begin{aligned}
 2.72 \quad P &= 10,000(P/F, 10\%, 20) \\
 &= 10,000(0.1486) \\
 &= \$1486
 \end{aligned}$$

Answer is (d)

$$\begin{aligned}
 2.73 \quad F &= 100,000(F/A, 18\%, 5) \\
 &= 100,000(7.1542) \\
 &= \$715,420
 \end{aligned}$$

Answer is (c)

$$\begin{aligned}
 2.74 \quad P &= 100,000(P/A, 10\%, 5) - 5000(P/G, 10\%, 5) \\
 &= 100,000(3.7908) - 5000(6.8618) \\
 &= \$344,771
 \end{aligned}$$

Answer is (a)

$$\begin{aligned}
 2.75 \quad F &= 20,000(F/P, 12\%, 10) \\
 &= 20,000(3.1058) \\
 &= \$62,116
 \end{aligned}$$

Answer is (a)

$$\begin{aligned}
 2.76 \quad A &= 100,000(A/P, 12\%, 5) \\
 &= 100,000(0.27741) \\
 &= \$27,741
 \end{aligned}$$

Answer is (b)

$$\begin{aligned}
 2.77 \quad A &= 100,000(A/F, 12\%, 3) \\
 &= 100,000(0.29635) \\
 &= \$29,635
 \end{aligned}$$

Answer is (c)

$$\begin{aligned}
 2.78 \quad A &= 10,000(F/A, 12\%, 25) \\
 &= 10,000(133.3339) \\
 &= \$1,333,339
 \end{aligned}$$

Answer is (d)

$$\begin{aligned}
 2.79 \quad F &= 10,000(F/P, 12\%, 5) + 10,000(F/P, 12\%, 3) + 10,000 \\
 &= 10,000(1.7623) + 10,000(1.4049) + 10,000 \\
 &= \$41,672
 \end{aligned}$$

Answer is (c)

$$\begin{aligned}
 2.80 \quad P &= 8,000(P/A, 10\%, 5) + 900(P/G, 10\%, 5) \\
 &= 8,000(3.7908) + 900(6.8618) \\
 &= \$36,502
 \end{aligned}$$

Answer is (d)

$$\begin{aligned}
 2.81 \quad 100,000 &= 20,000(P/A, i, 10) \\
 (P/A, i, 10) &= 5.000 \\
 i &\text{ is between 15 and 16\%} \\
 \text{Answer is (a)}
 \end{aligned}$$

$$\begin{aligned}
 2.82 \quad 60,000 &= 15,000(P/A, 18\%, n) \\
 (P/A, 18\%, n) &= 4.000 \\
 n &\text{ is between 7 and 8} \\
 \text{Answer is (b)}
 \end{aligned}$$

## Case Study Solution

### I. Manhattan Island

Simple interest

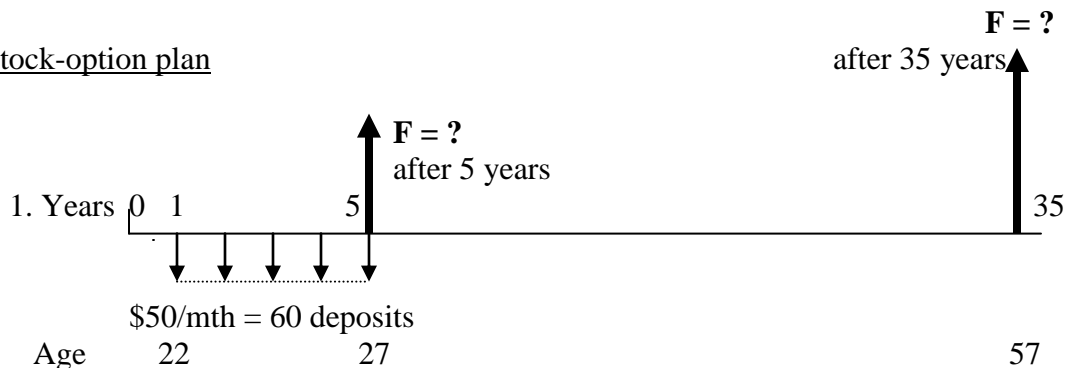
$n = 375$  years from 1626 – 2001

$$\begin{aligned}
 P + I &= P + nPi = 375(24)(.06) + 24 \\
 &= P(1 + ni) = 24(1 + 375(.06)) \\
 &= \$564
 \end{aligned}$$

Compound interest

$$\begin{aligned}
 F &= P(F/P, 6\%, 375) \\
 &= 24(3,088,157,729.0) \\
 &= \$74,115,785,490, \text{ which is } \$74+ \text{ billion}
 \end{aligned}$$

### II. Stock-option plan



2. Value when leaving the company

$$\begin{aligned} F &= A(F/A, 1.25\%, 60) \\ &= 50(88.5745) \\ &= \$4428.73 \end{aligned}$$

3. Value at age 57 ( $n = 30$  years)

$$\begin{aligned} F &= P(F/P, 15\%, 30) \\ &= 4428.73(66.2118) \\ &= \$293,234 \end{aligned}$$

4. Amount for 7 years to accumulate  $F = \$293,234$

$$\begin{aligned} A &= F(A/F, 15\%, 7) \\ &= 293,234(.09036) \\ &= \$26,497 \text{ per year} \end{aligned}$$

5. Amount in 20's:  $5(12)50 = \$3000$   
Amount in 50's:  $7(26,497) = \$185,479$